

# Sound Synthesis

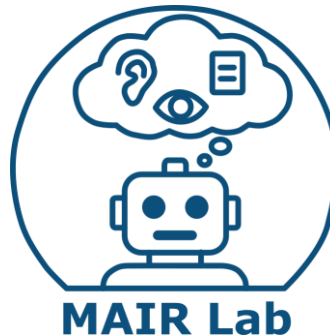
안인규 (Inkyu An)

**Speech And Audio Recognition**  
(오디오 음성인식)

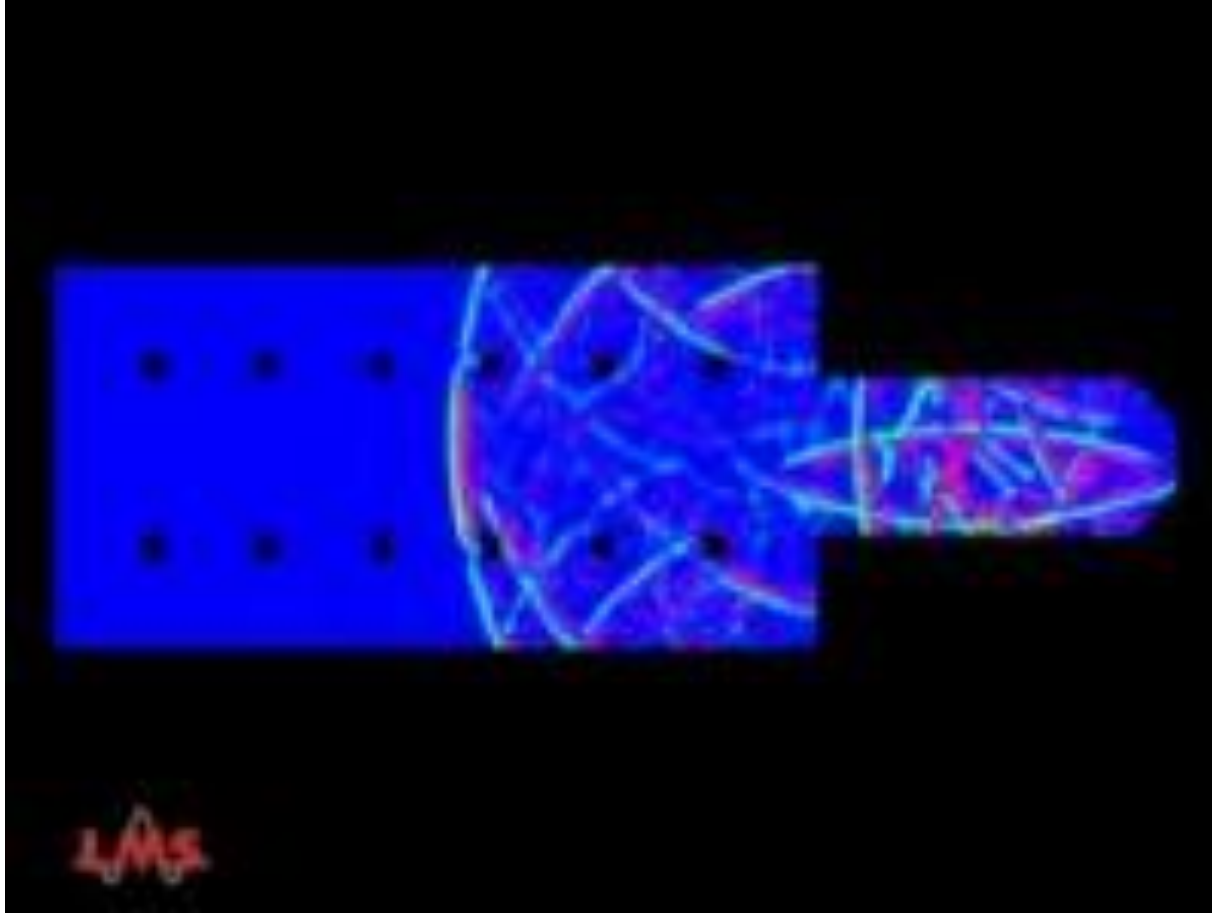
<https://mairlab-km.github.io/>



This lecture material is based on the Lecture Notes (EE837) of Prof. Jung-Woo Choi at KAIST and the Ph.D. dissertation of Dr. Taeyoung Kim at Samsung Electronics



# How does sound propagate?

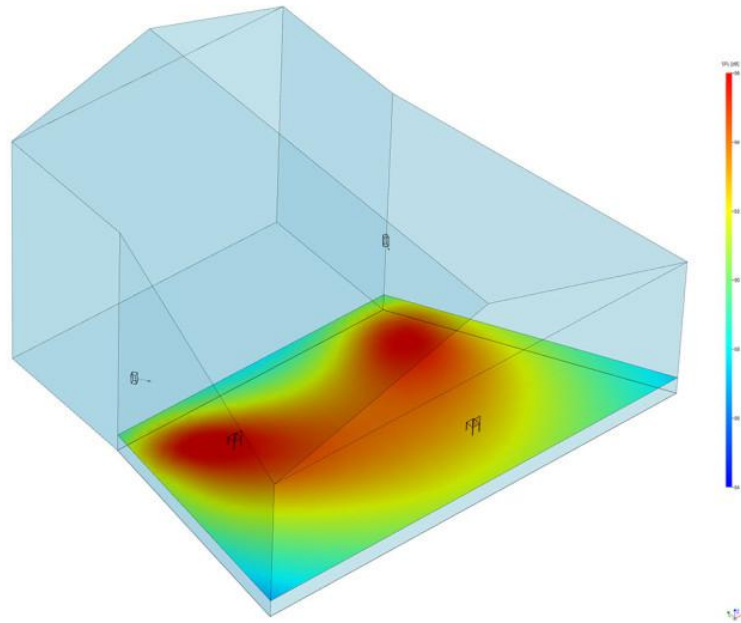


<https://www.youtube.com/watch?v=Xsx4VBEKciA>



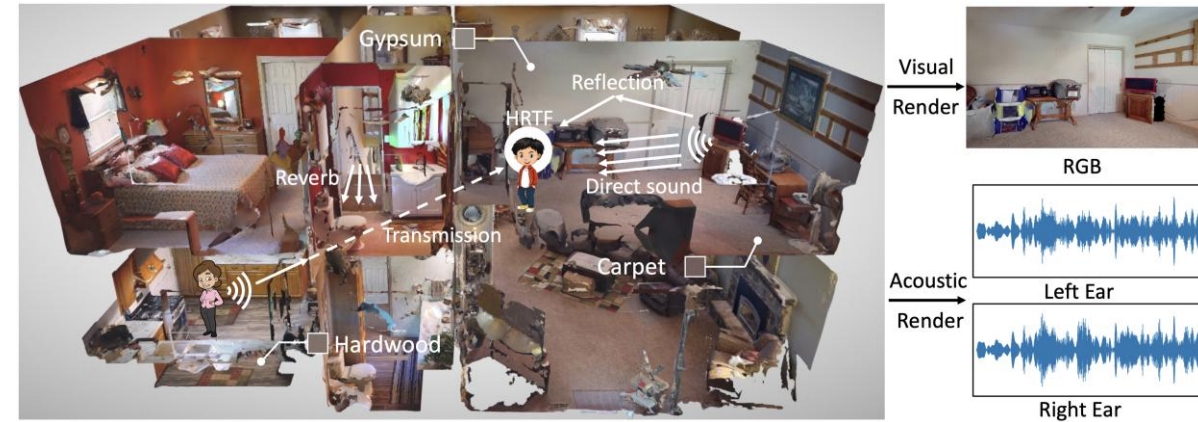
<https://www.youtube.com/shorts/GnAvquGBmnY>

# To create realistic sound!



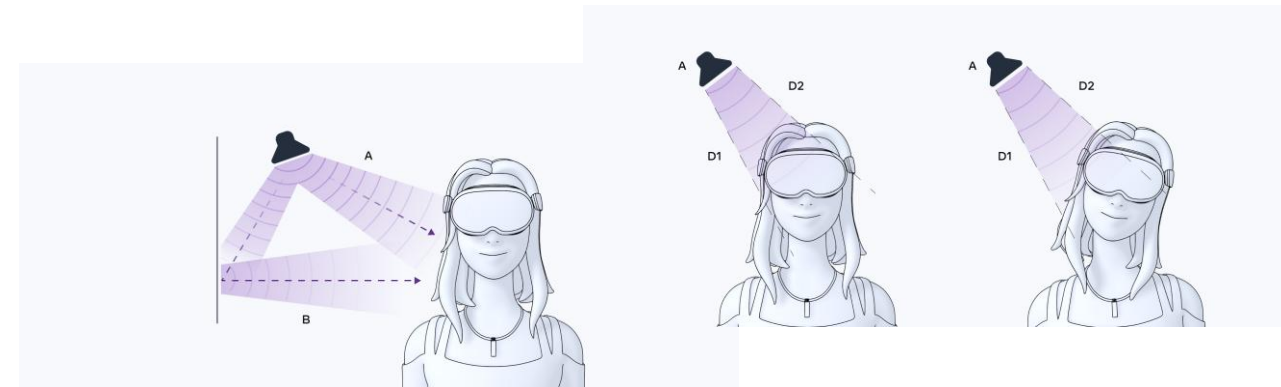
Acoustic simulation (designing Auditorium)

<https://audioxpress.com/article/acoustic-simulation-ease-5-s-acousteer-engine-redefines-design-workflows>



Sound simulation (generating synthetic data)

<https://vision.cs.utexas.edu/projects/soundspace2/>



Sound simulation (Spatial audio in VR)

[https://developers.meta.com/horizon/design/spatial\\_audio/](https://developers.meta.com/horizon/design/spatial_audio/)

# To create realistic sound!



Recorded sound in the real environment

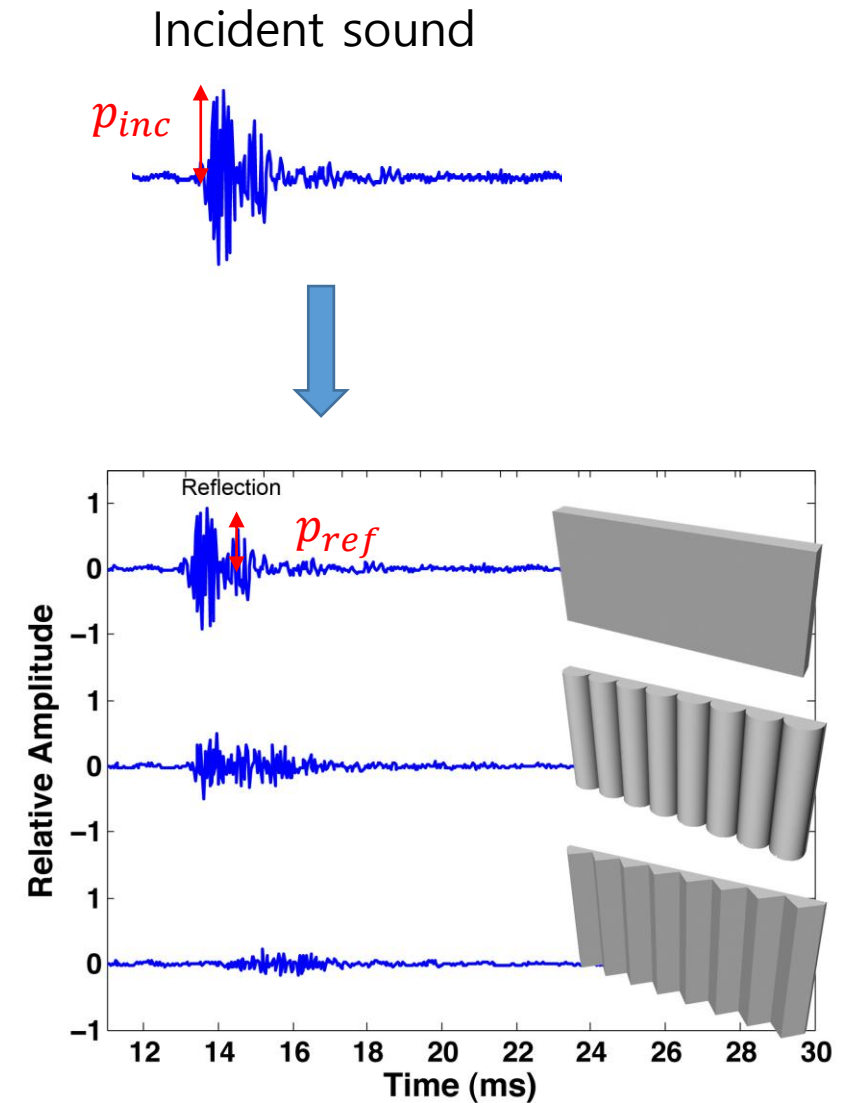
Without considering  
acoustic material

Generated sound in the virtual environment

Using appropriate  
acoustic material

# Reflection

- If reflection occurs, what happens?
  - If the wall is a rigid body, It should be a fixed boundary condition
- How will the sound intensity change?
  - Reflection coefficient:  $R_p = \frac{p_{ref}}{p_{inc}}$
  - Reflection coefficient는 material마다 다르다!



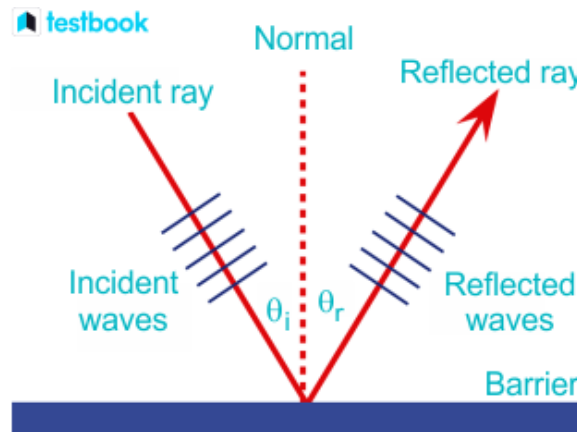
# Reflection

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$$p_{inc}(x, t) = Ae^{i(kx - \omega t)}$$



$$p_{ref}(x, t) = R_p \cdot p_{inc}(-x, t) \cdot e^{i\pi}$$

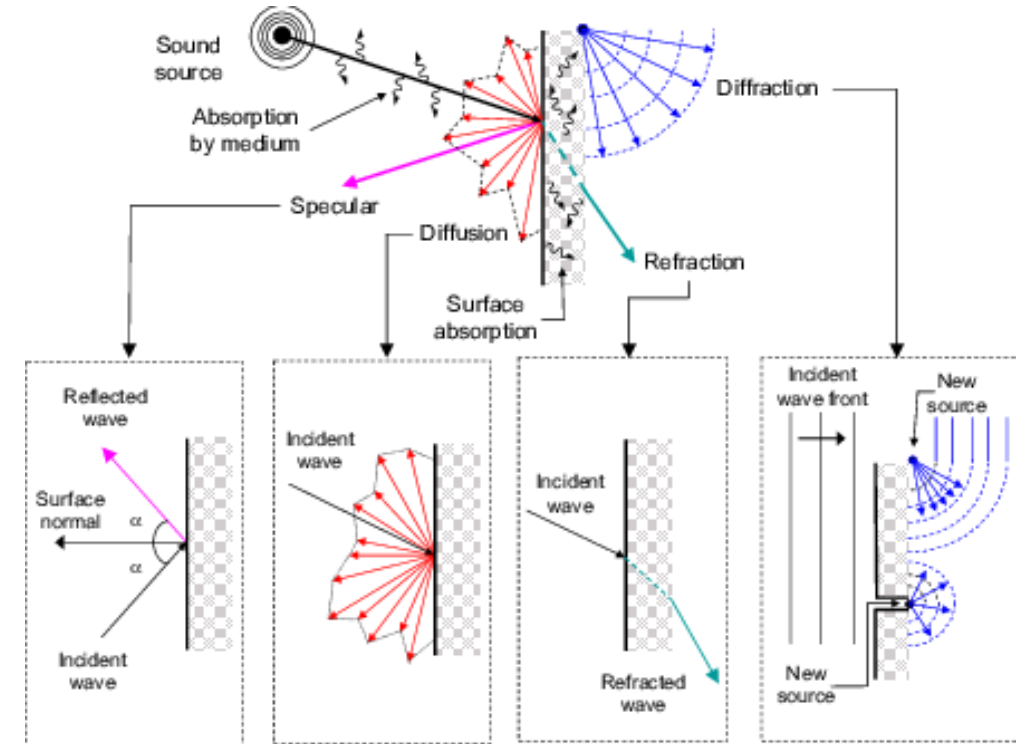
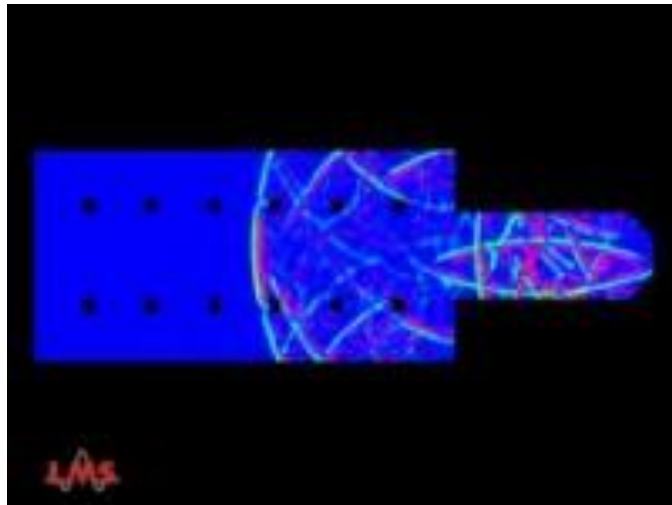


Reflection law

# Reflection

- If reflection occurs, what happens?
  - If the wall is a rigid body, It should be a fixed boundary condition

소리가 물체에 충돌할 때, specular reflection (정반사) 뿐만 아니라, **Diffuse, refraction, diffraction** 등이 함께 발생한다.

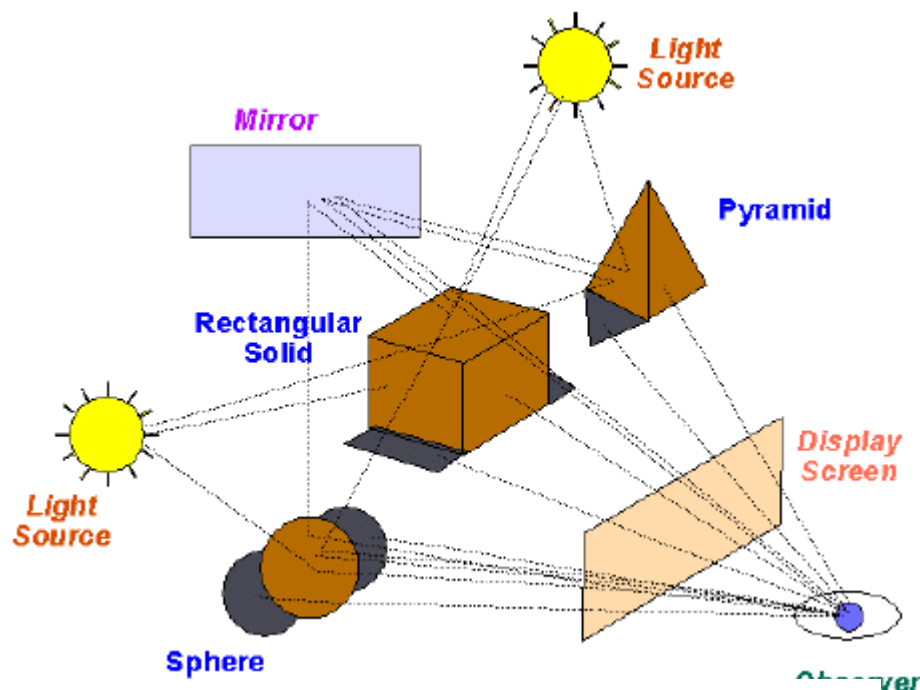


이를 정확하게 Simulation하는 것은 매우 시간이 많이 걸린다.

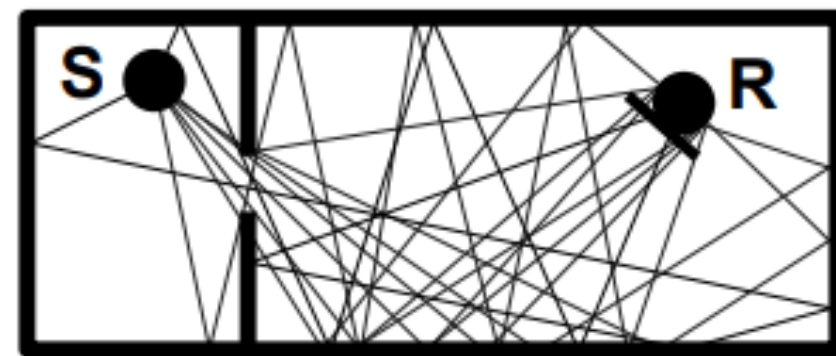


# Geometrical Acoustics

- **Geometrical Acoustics:** 음파를 직선으로 진행하는 광선처럼 모델링하여 반사, 흡수, 산란을 다루는 음향 모델링 방법
  - 파동 방정식을 직접 풀지 않고, 고주파 근사(high-frequency approximation)를 사용하여 음파를 빔처럼 다루는 방법



Ray tracing (Computer Graphics)

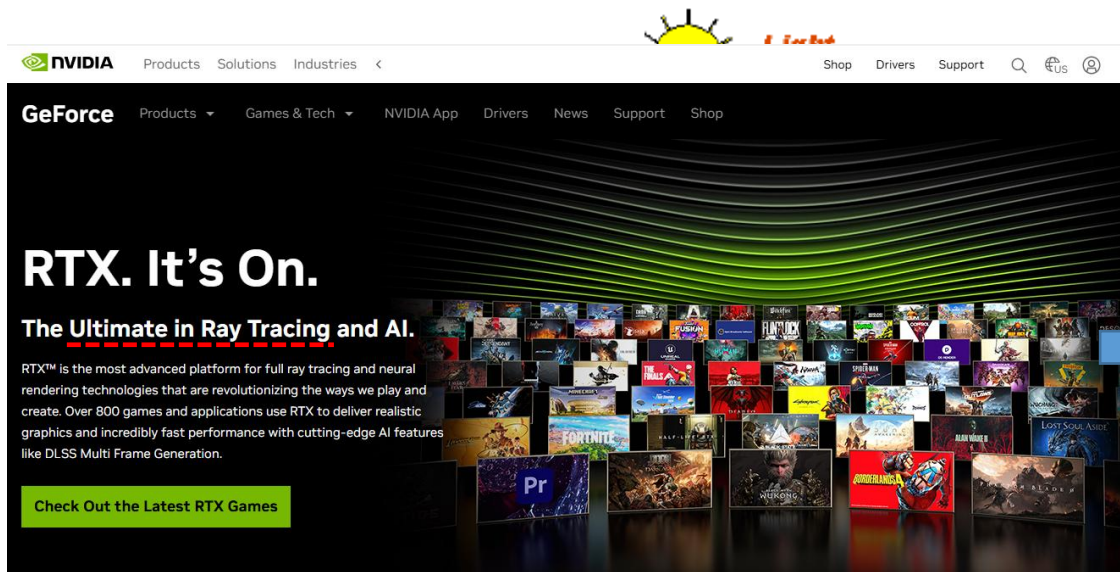


Sound propagation paths

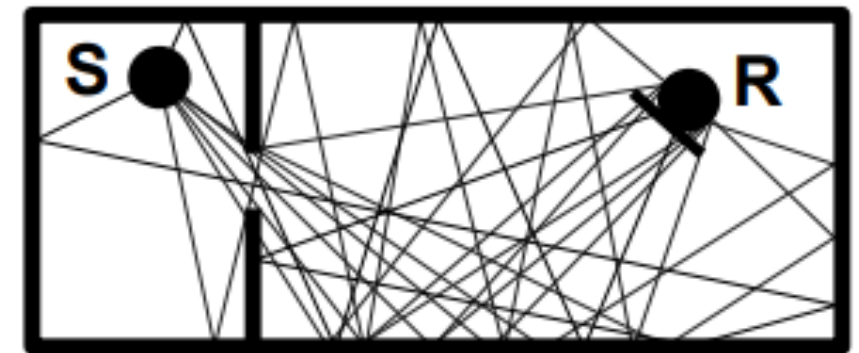


# Geometrical Acoustics

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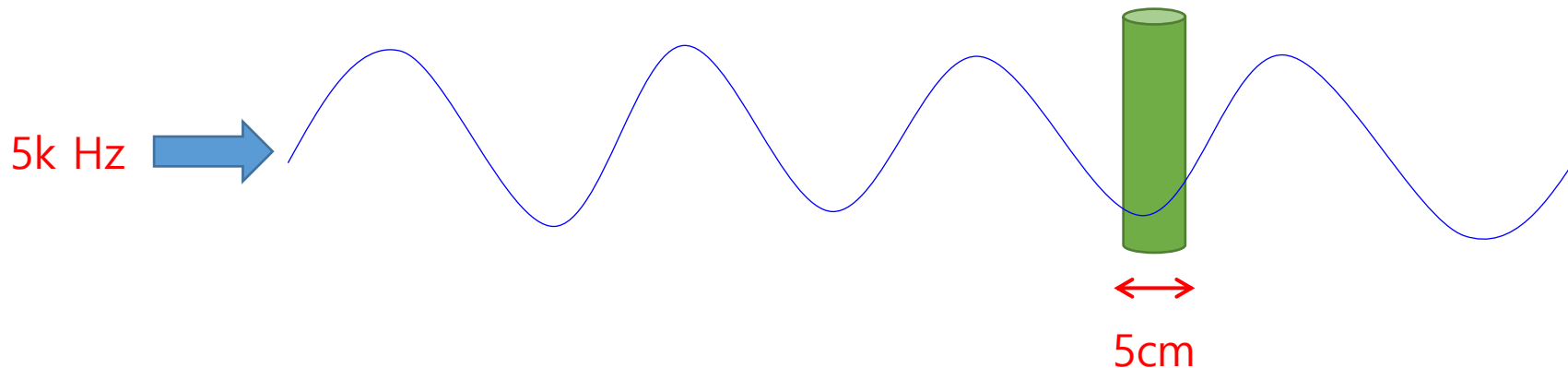
Sphere  
Ray tracing (Computer Graphics)



Sound propagation paths

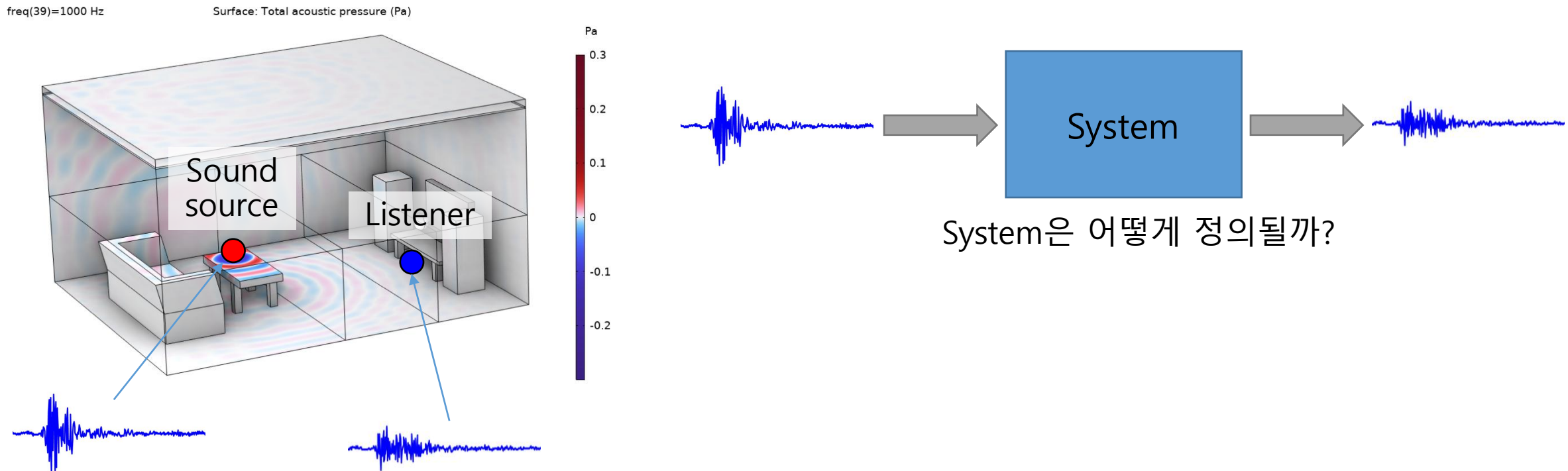
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  - 파동 방정식을 직접 풀지 않고, 고주파 근사(high-frequency approximation)를 사용하여 음파를 빔처럼 다루는 방법
  - **High-frequency assumption:** 파장이 장애물 크기보다 훨씬 작을 때  $\lambda \ll D$  (예: 5kHz 의 파장은 대략 7cm,  $f = \frac{c}{\lambda}$ )
  - 만약 High-frequency assumption을 만족하지 않는다면, 회절이 dominant해짐



# Sound Propagation System

- Sound Propagation System in Geometrical Acoustics
  - **Input:** sound source에서 발생한 소리
  - **Output:** Listener가 들을 소리

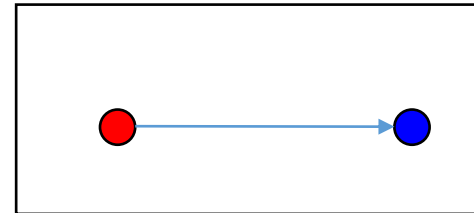
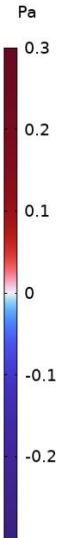
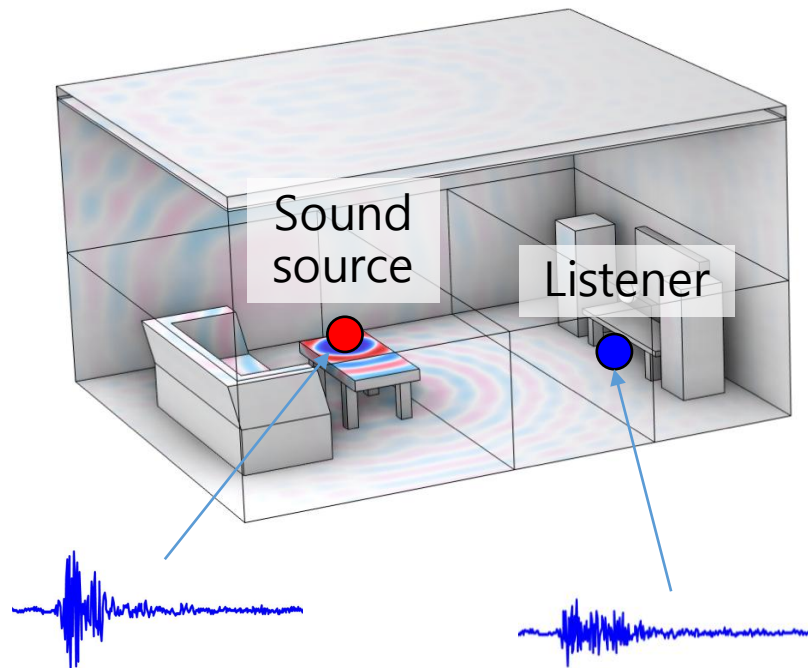


# Sound Propagation System

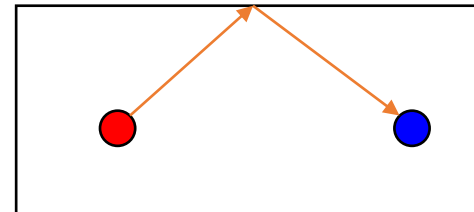
- Sound Propagation System

freq(39)=1000 Hz

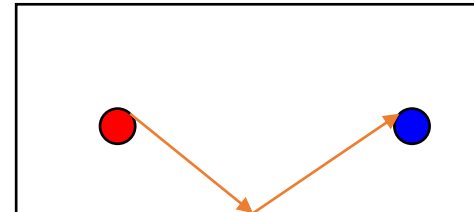
Surface: Total acoustic pressure (Pa)



Direct path

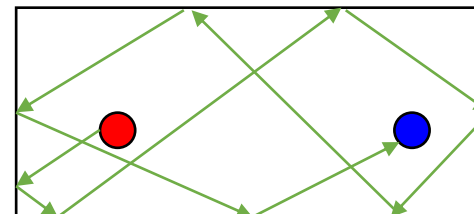


1-st order reflection



1-st order reflection

⋮



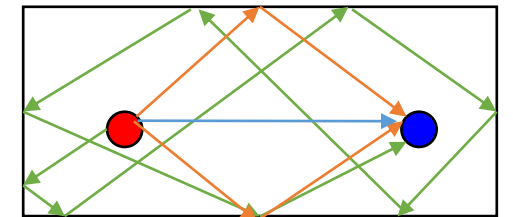
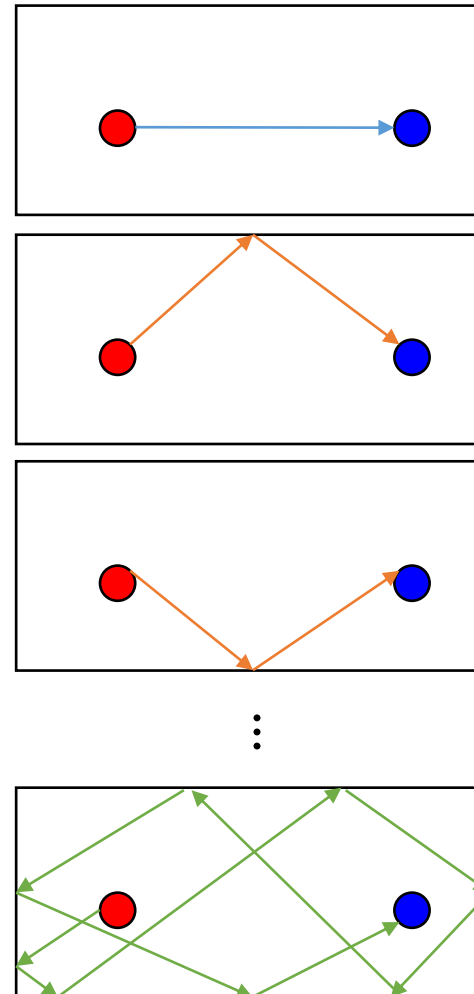
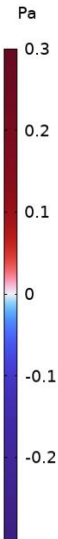
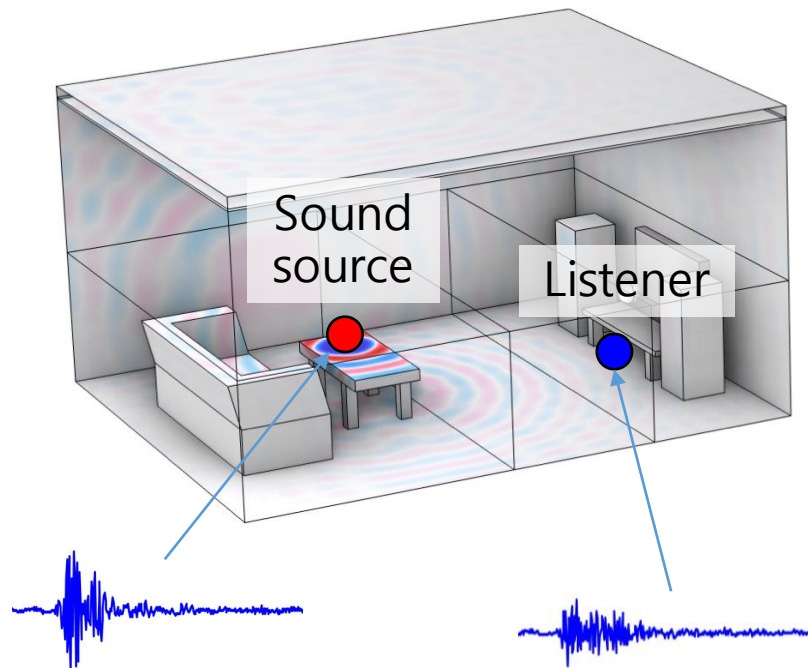
n-th order reflection

# Sound Propagation System

- Sound Propagation System

freq(39)=1000 Hz

Surface: Total acoustic pressure (Pa)



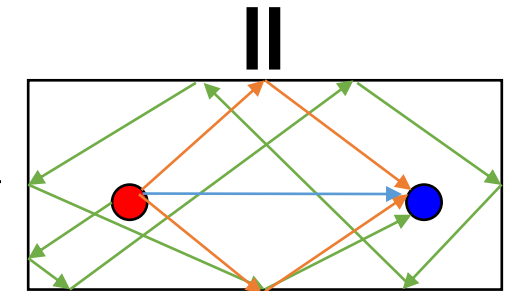
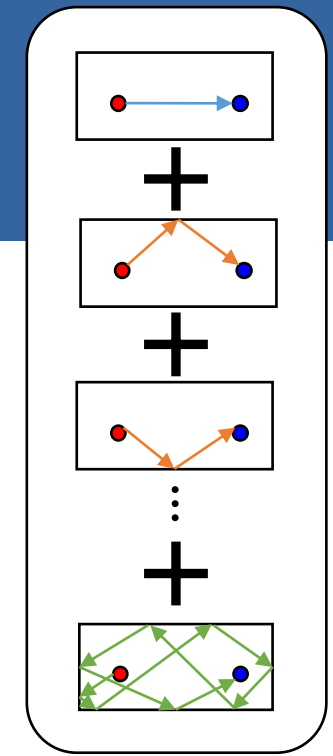
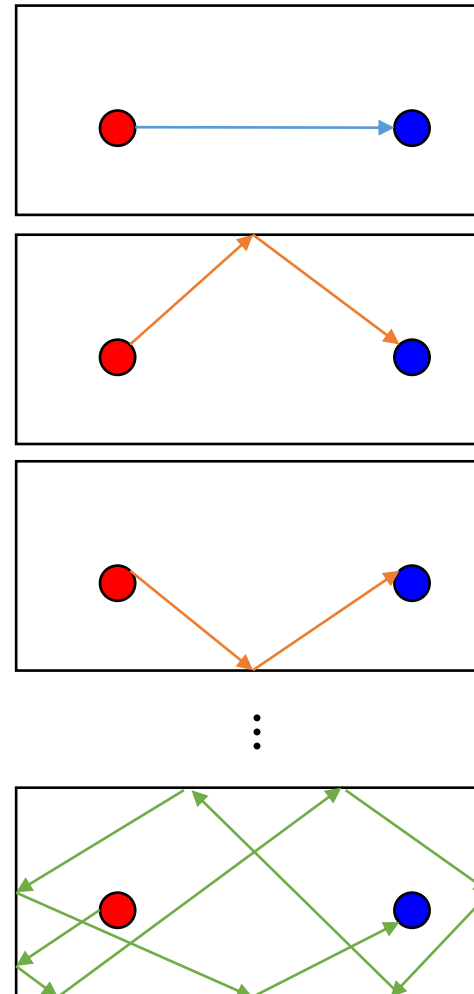
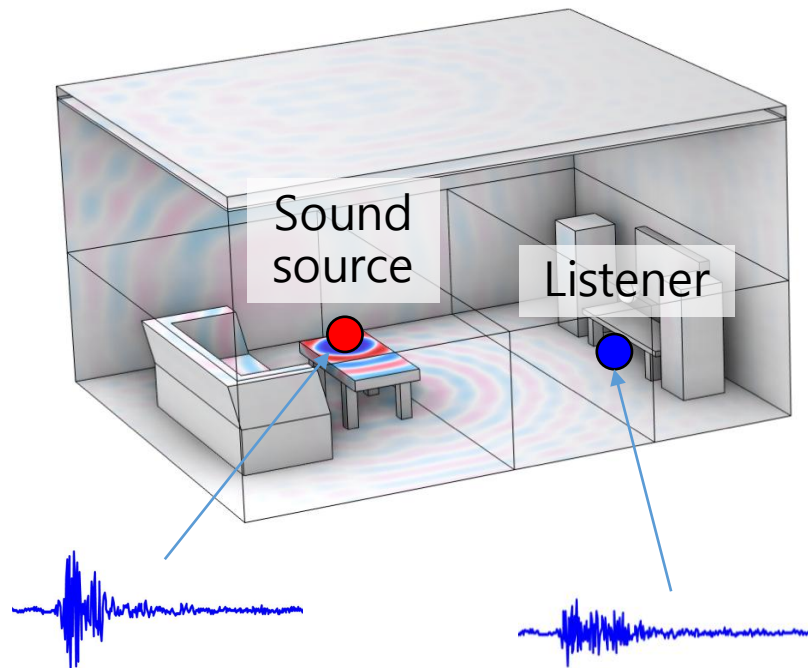
실제로는 여러 경로가 하나의 공간에서 동시에 진행

# Sound Propagation System

- Sound Propagation System

freq(39)=1000 Hz

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실제로는 여러 경로가 하나의 공간에서 동시에 진행

# Sound Propagation System: LTI system

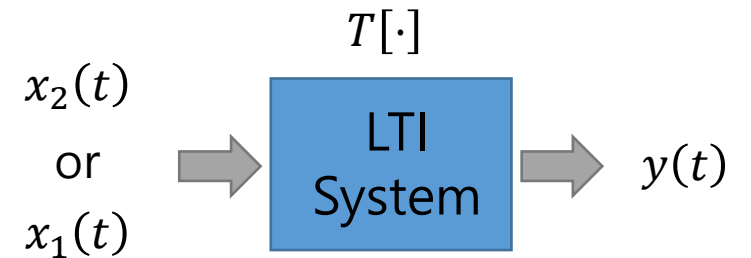
- LTI (Linear Time-Invariant) system  
: Linearity와 Time invariance를 만족

- Linearity

- Additivity:  $T[x_1(t) + x_2(t)] = T[x_1(t)] + T[x_2(t)]$

- scaling:  $T[ax(t)] = aT[x(t)]$

- Time invariance:  $x(t - t_0) \rightarrow y(t - t_0)$





# Sound Propagation System: LTI system

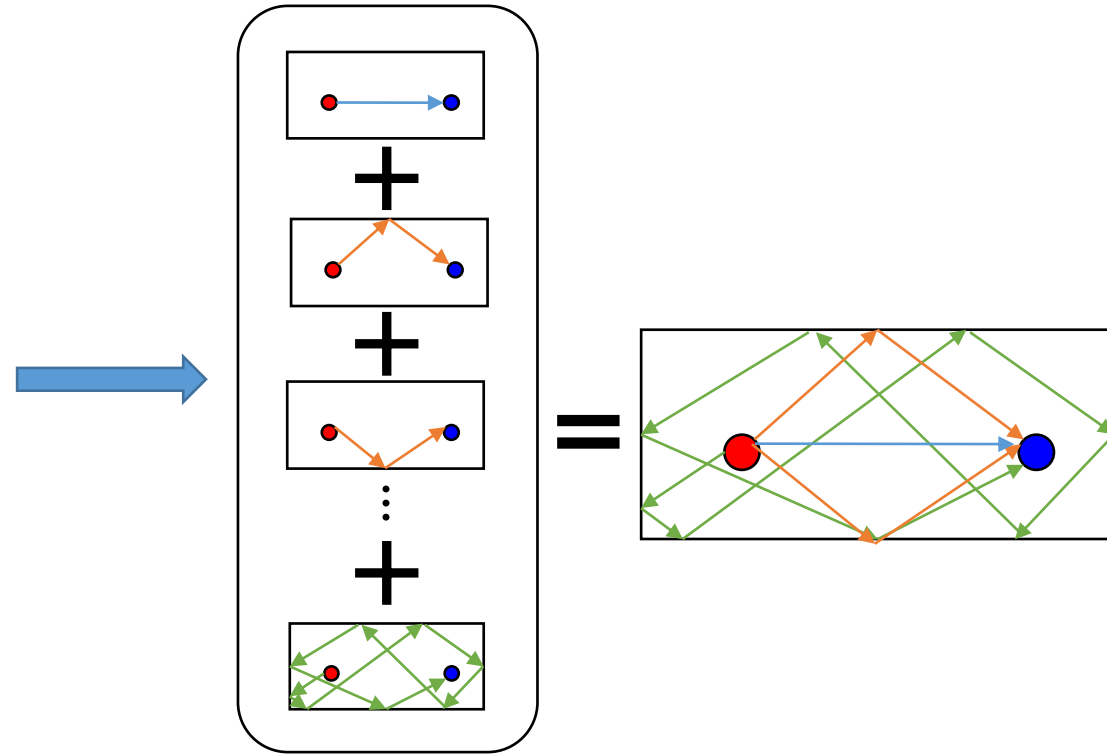
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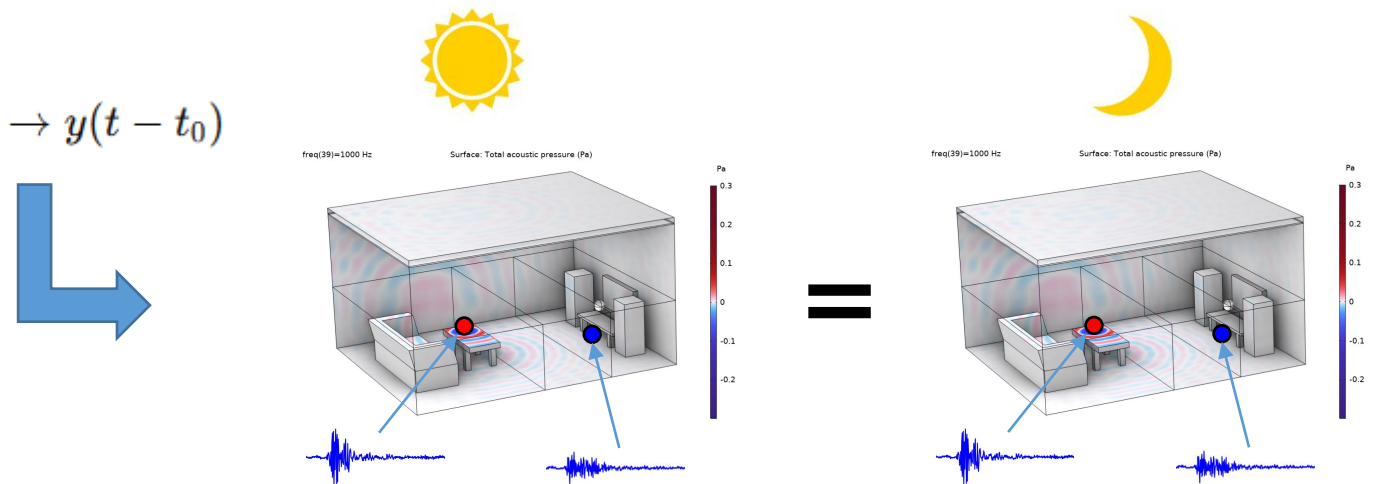
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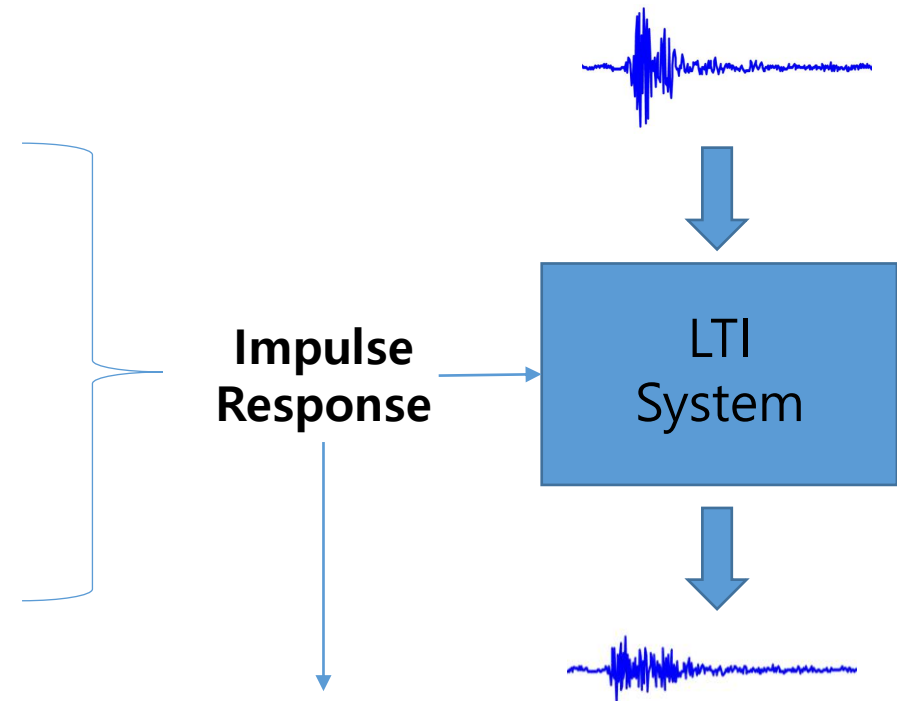
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Output은 Input과 Impulse Response  
의 Convolution으로 정의

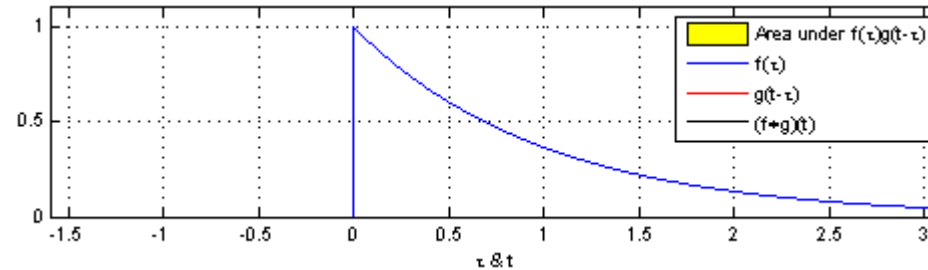
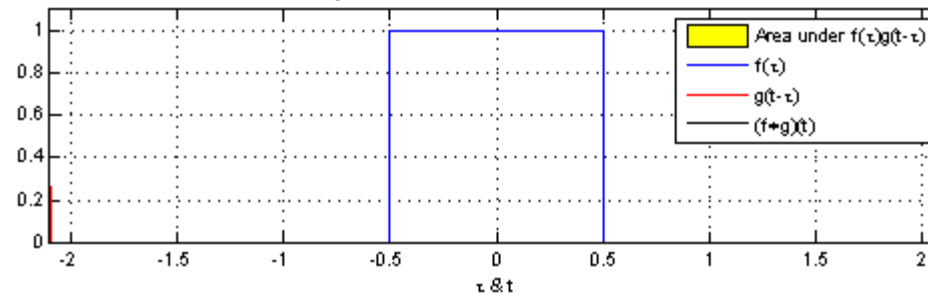
$$y(t) = \int_{-\infty}^{\infty} x(\tau)h(t - \tau)d\tau = x(t) * h(t)$$

# Sound Propagation System: LTI system

- Continuous-Time Convolution:

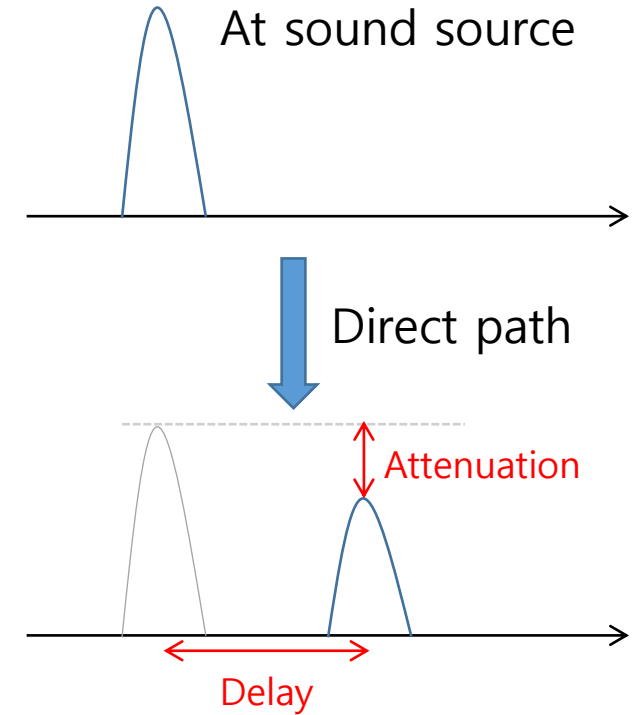
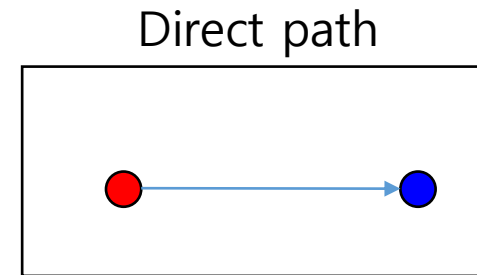
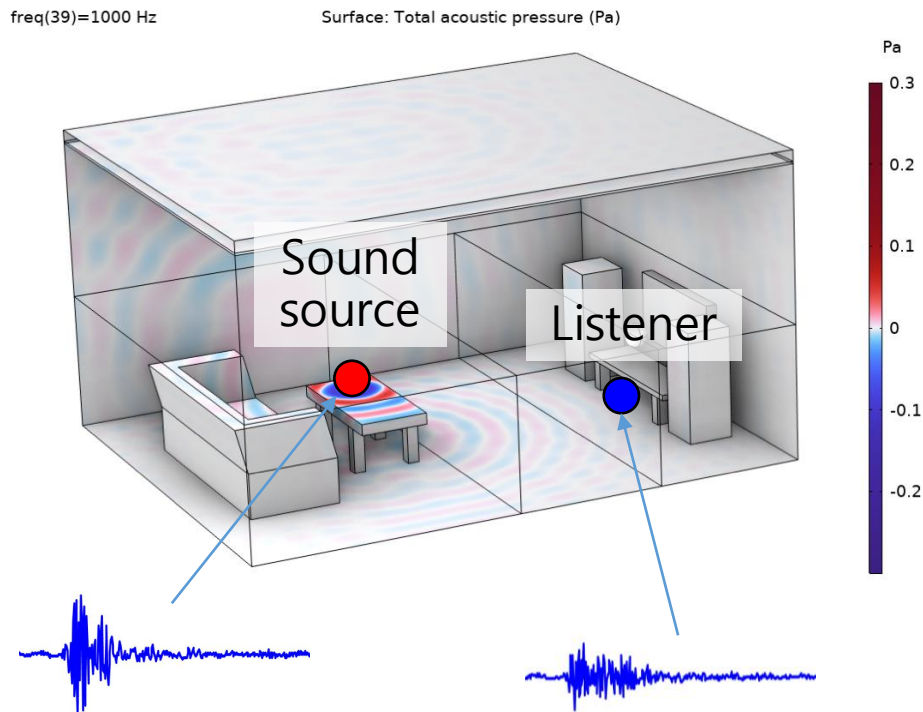
- $x * h = \int_{-\infty}^{\infty} x(\tau)h(t - \tau)d\tau$

Example of Convolution



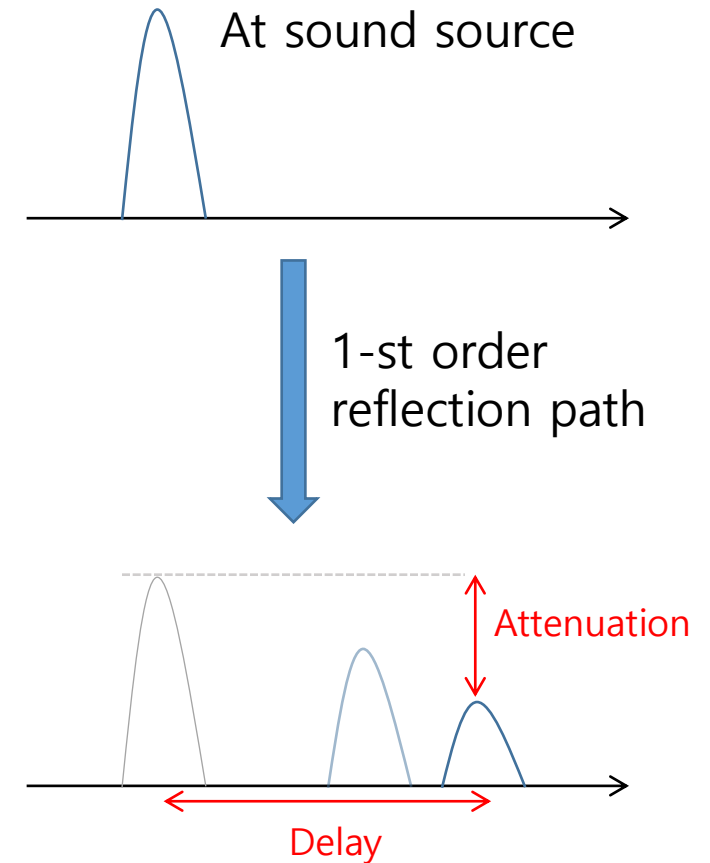
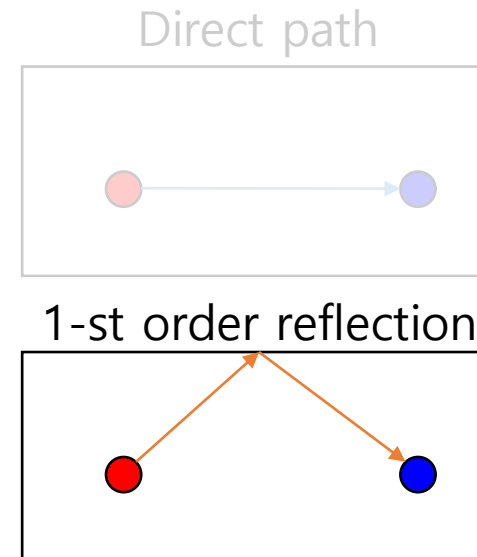
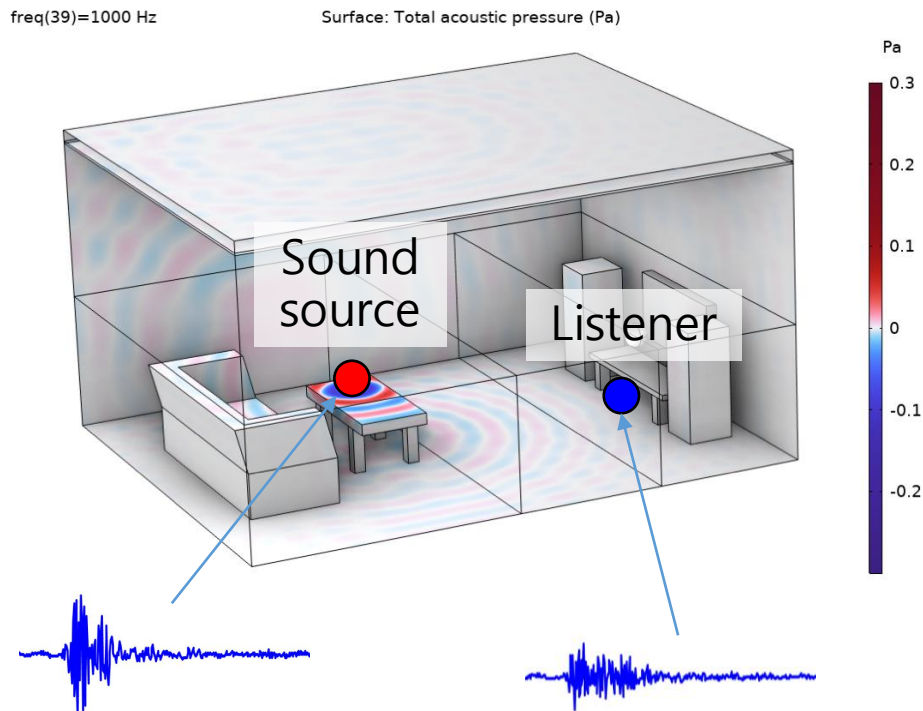
# Sound Propagation System: Impulse Response

- Sound Propagation System
  - Estimating Impulse response



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- Sound Propagation System
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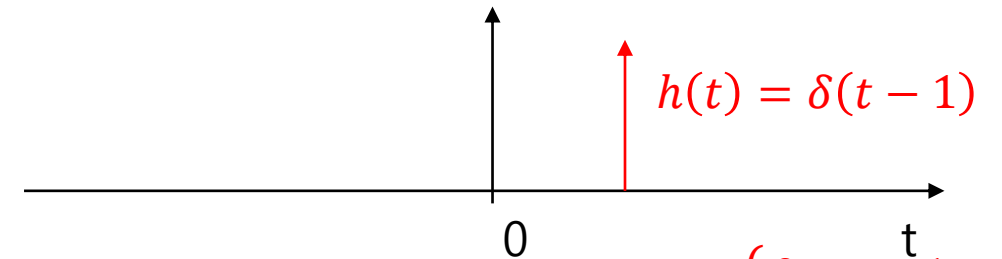
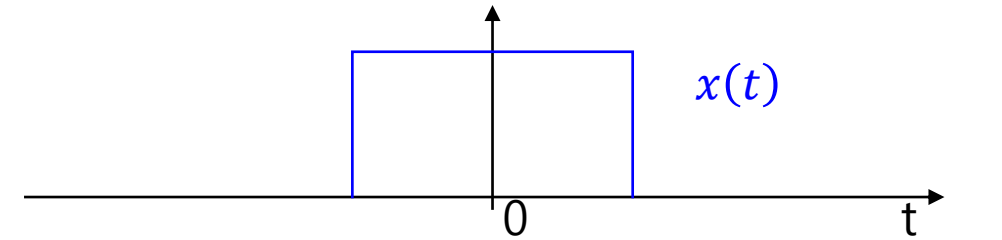
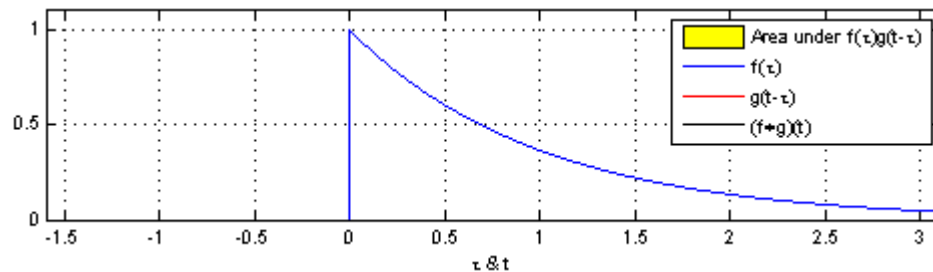
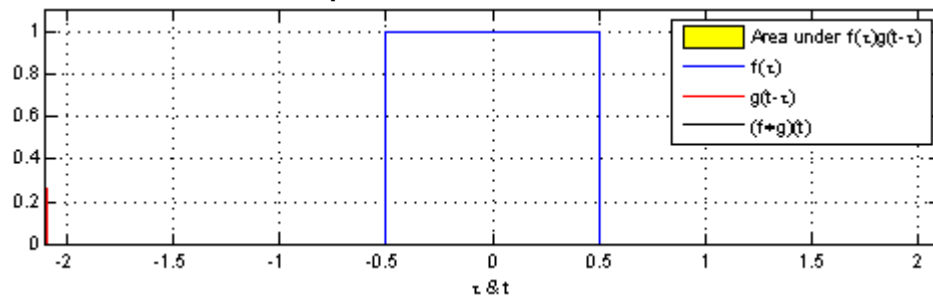


# Sound Propagation System: Impulse Response

- Continuous-Time Convolution:

- $$x * h = \int_{-\infty}^{\infty} x(\tau)h(t - \tau)d\tau$$

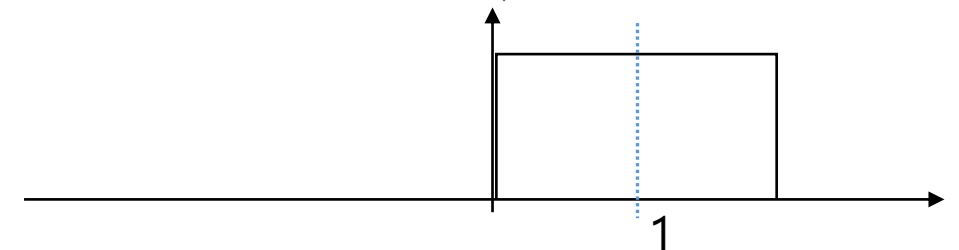
Example of Convolution



Dirac delta function  $\delta(t-1) = \begin{cases} 0, & t \neq 1 \\ \infty, & t = 1 \end{cases}$

$$\int_{-\infty}^{\infty} \delta(t-1)dt = 1$$

$(f * g)(t)?$

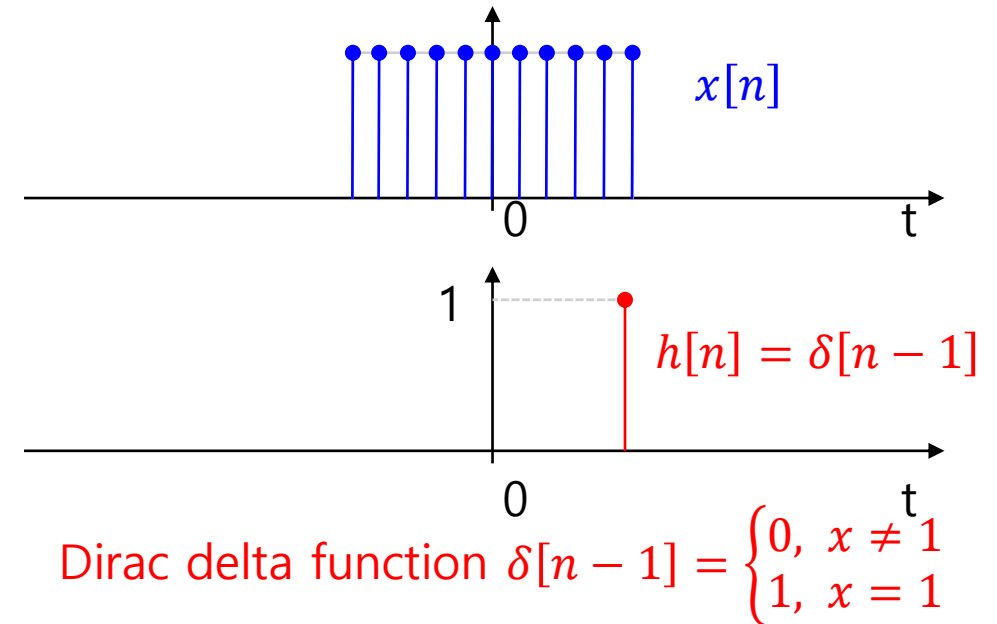
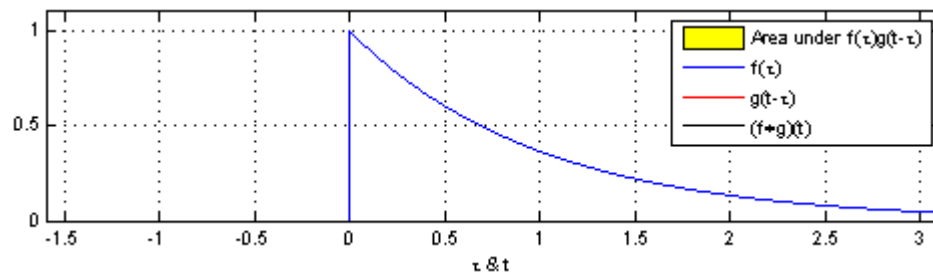
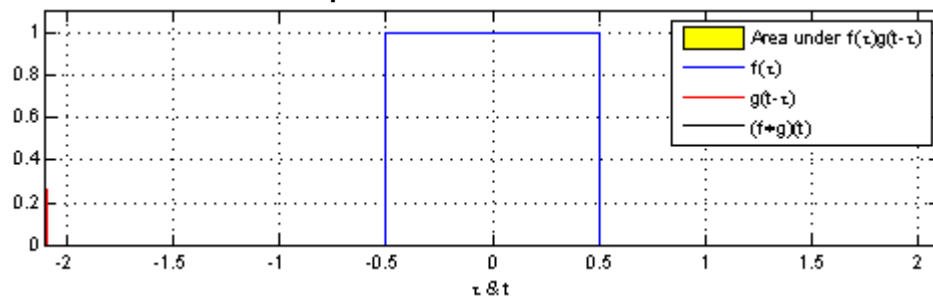




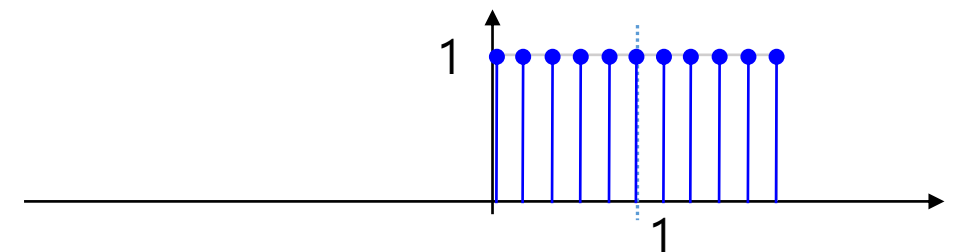
# Sound Propagation System: Impulse Response

- Discrete-Time Convolution:
  - $(x * h)[n] = \sum_{k=-\infty}^{\infty} x[k]h[n - k]$

Example of Convolution



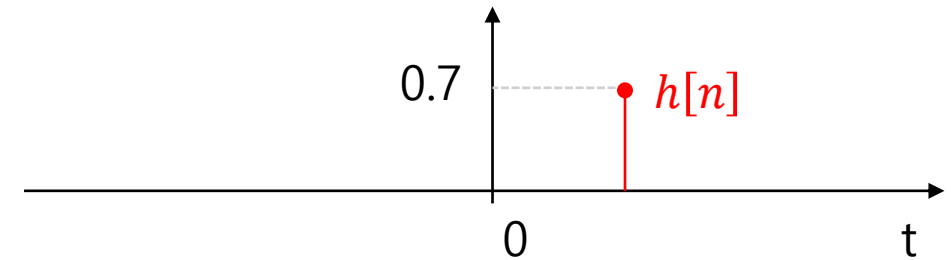
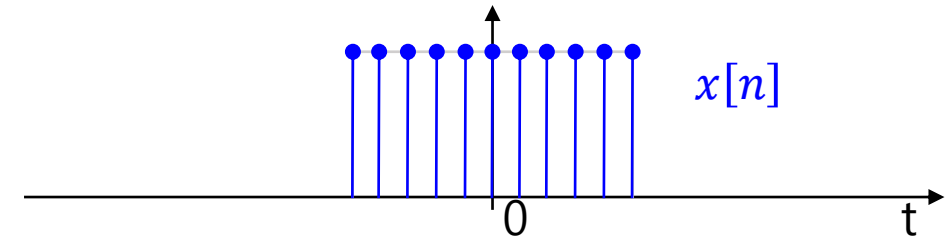
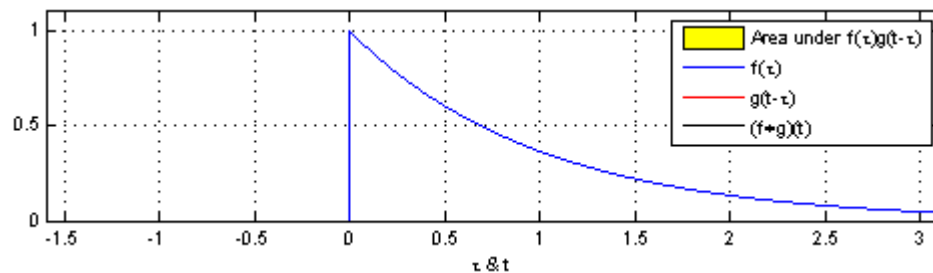
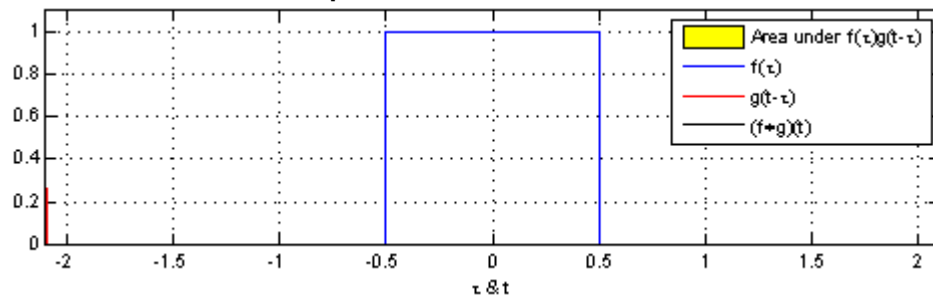
↓  $(f * g)[n]?$



# Sound Propagation System: Impulse Response

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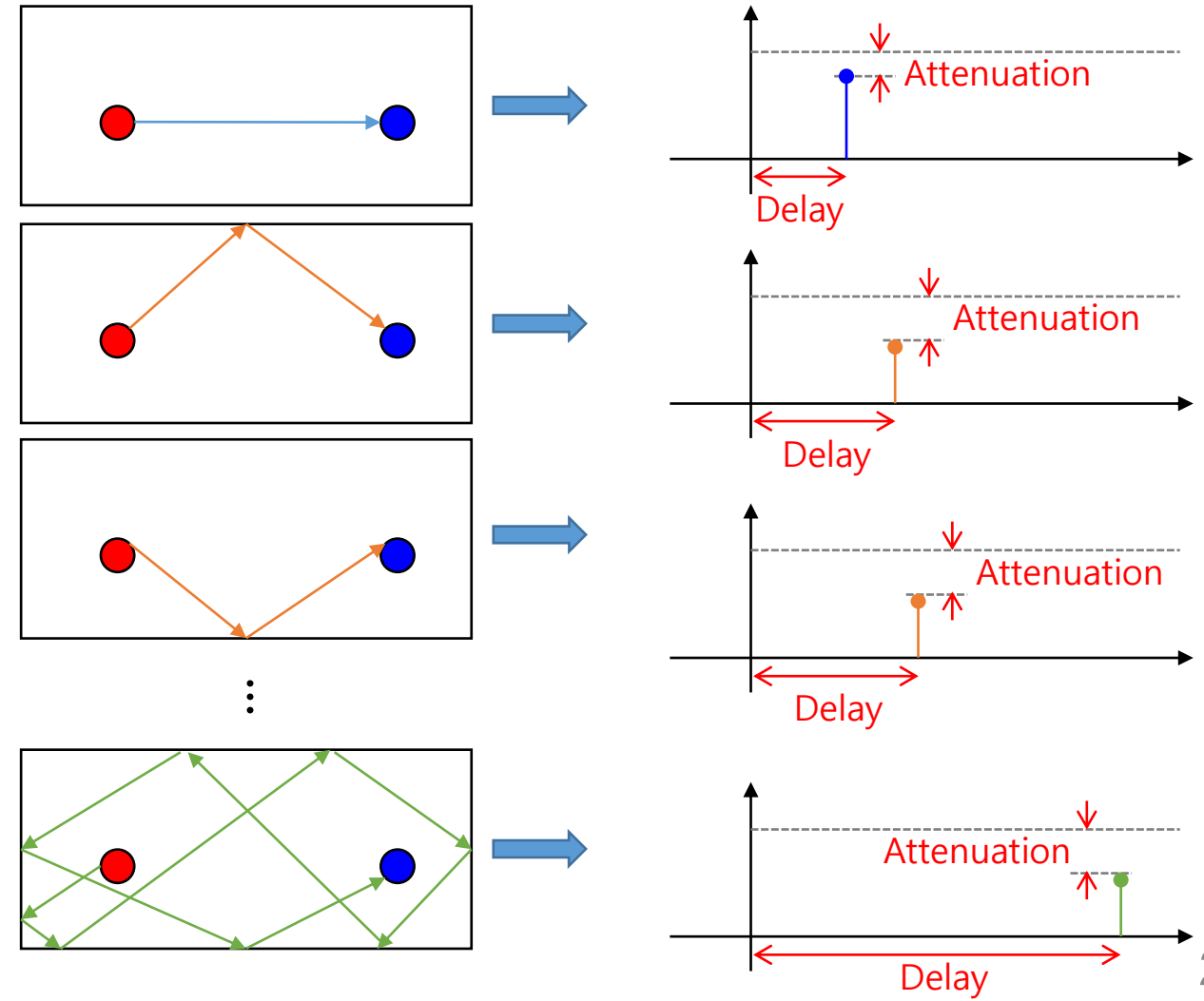
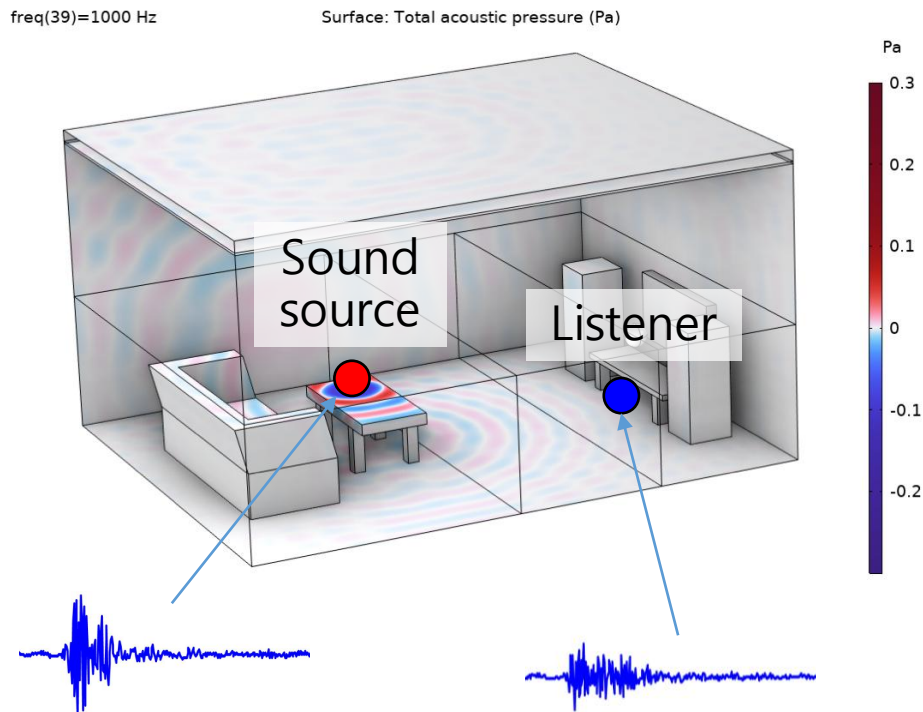
Example of Convolution



$(f * g)[n]?$

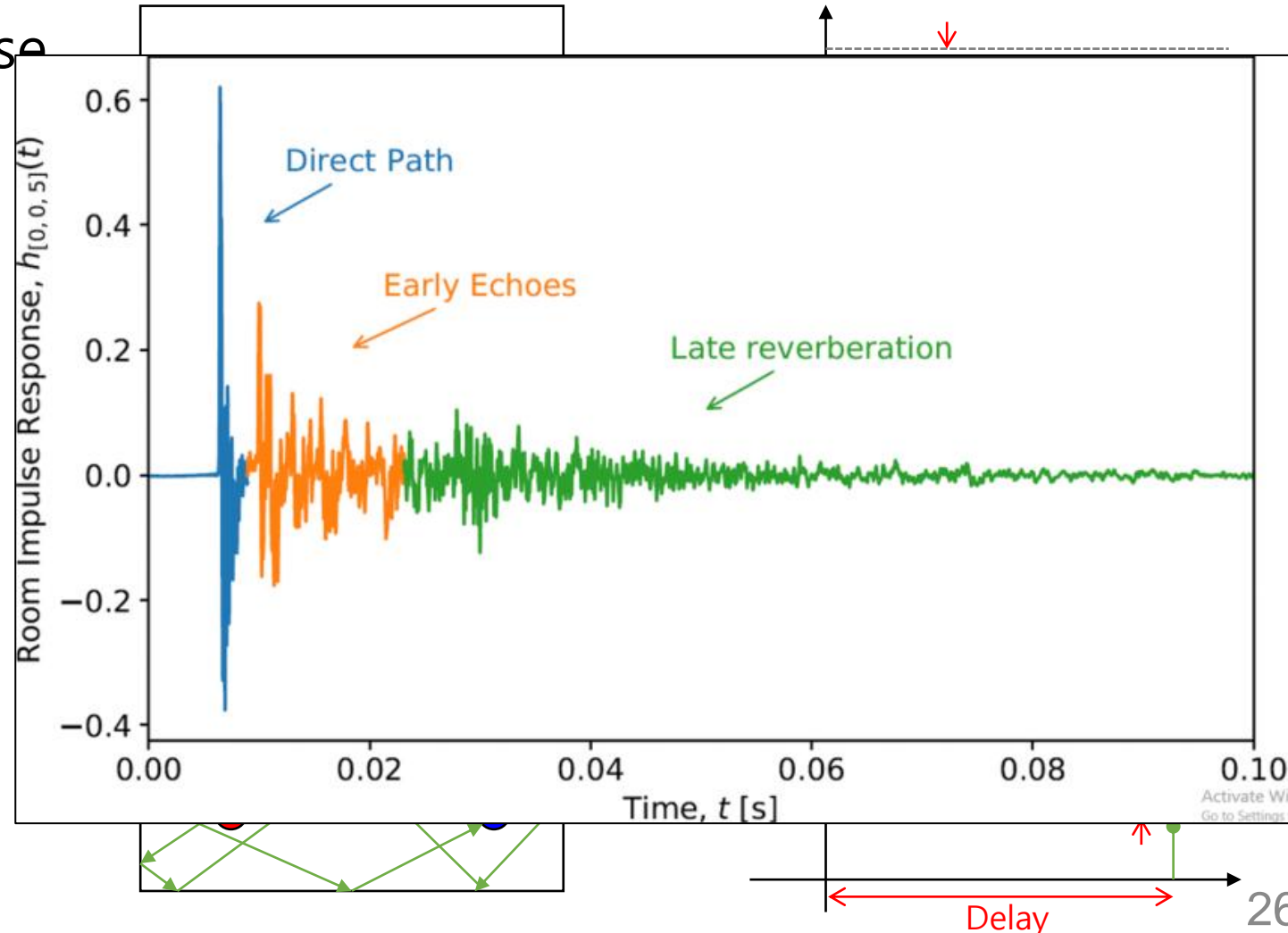
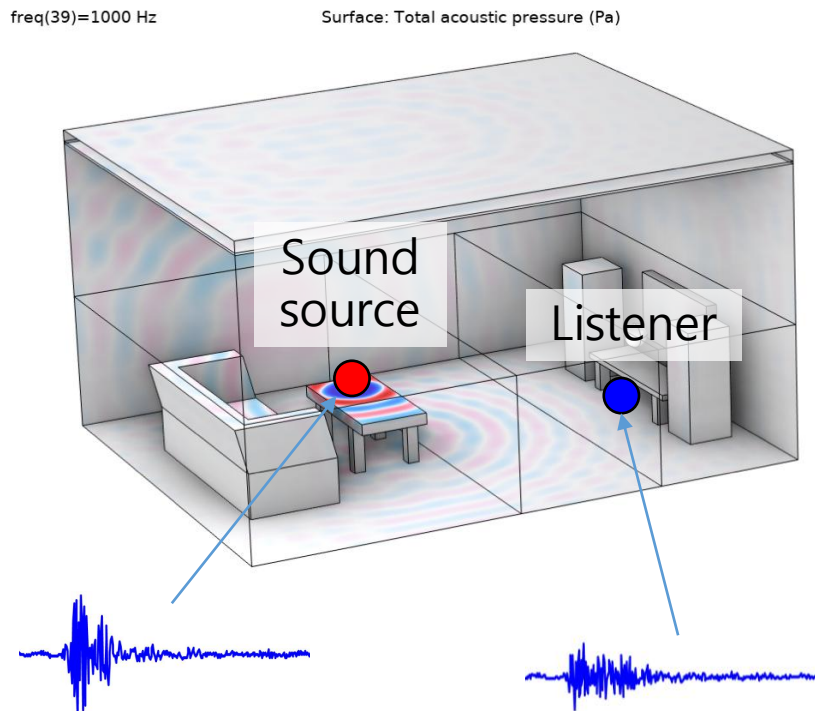
# Sound Propagation System: Impulse Response

- Sound Propagation System
  - Estimating Impulse response



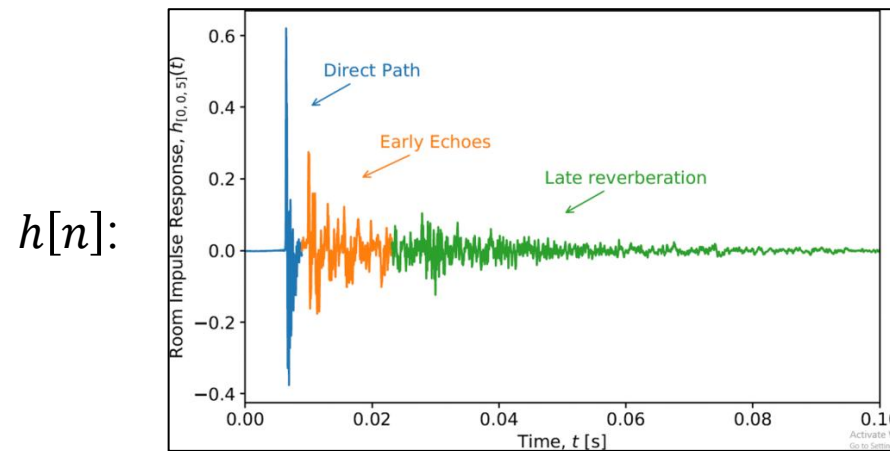
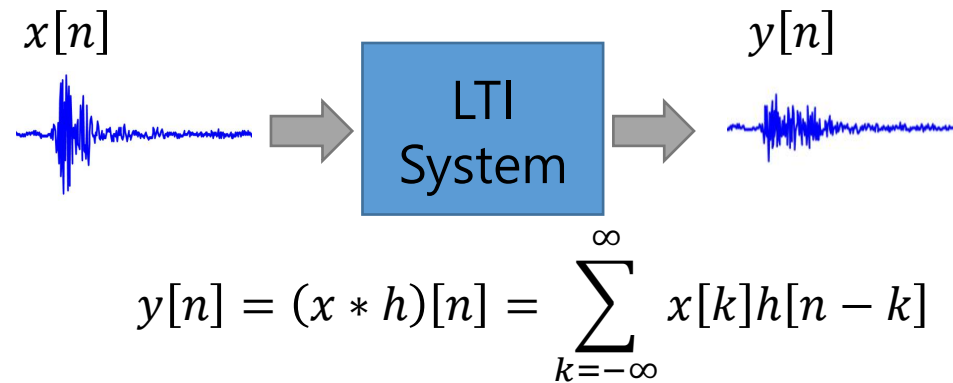
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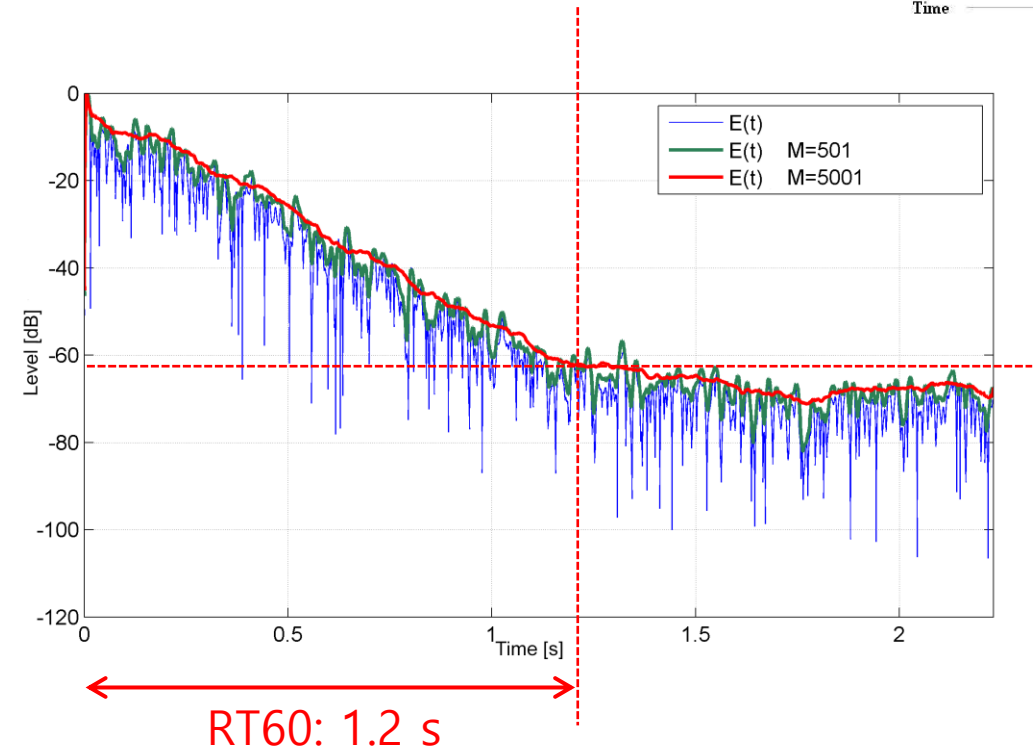
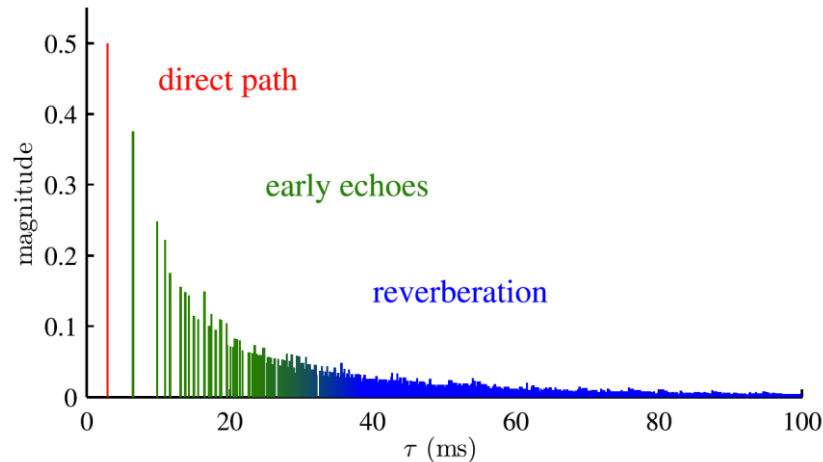
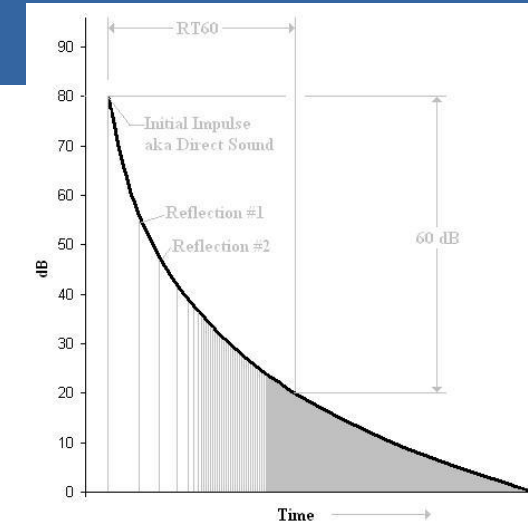
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- Sound Propagation System
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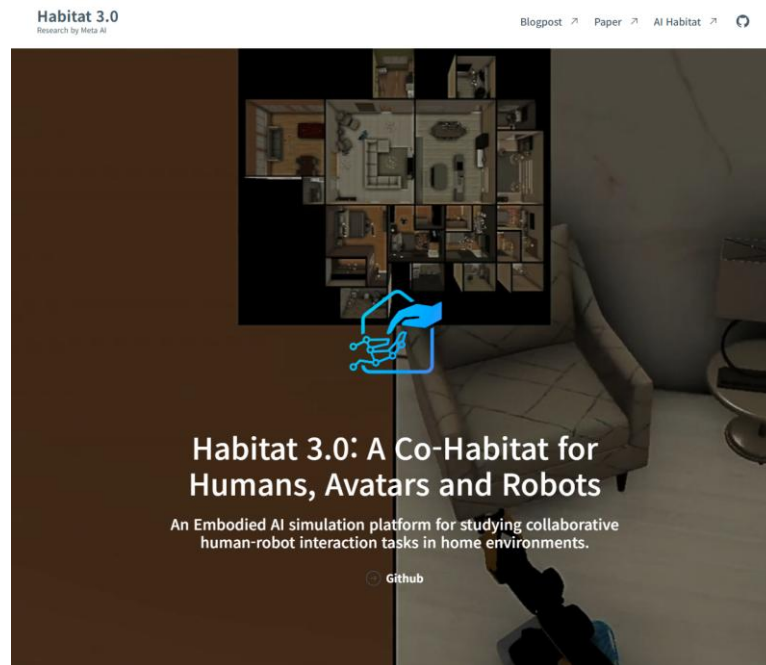
# Sound Propagation System: Reverberation

- Reverberation Time (RT60)
  - 소리의 울림이 큰 공간에서는 Reverberation Time이 증가
  - 소리의 울림이 작은 공간에서는 Reverberation Time이 감소
  - **RT60: Sound Pressure Level (SPL)이 60dB 만큼 감쇄되는 데 걸리는 시간**

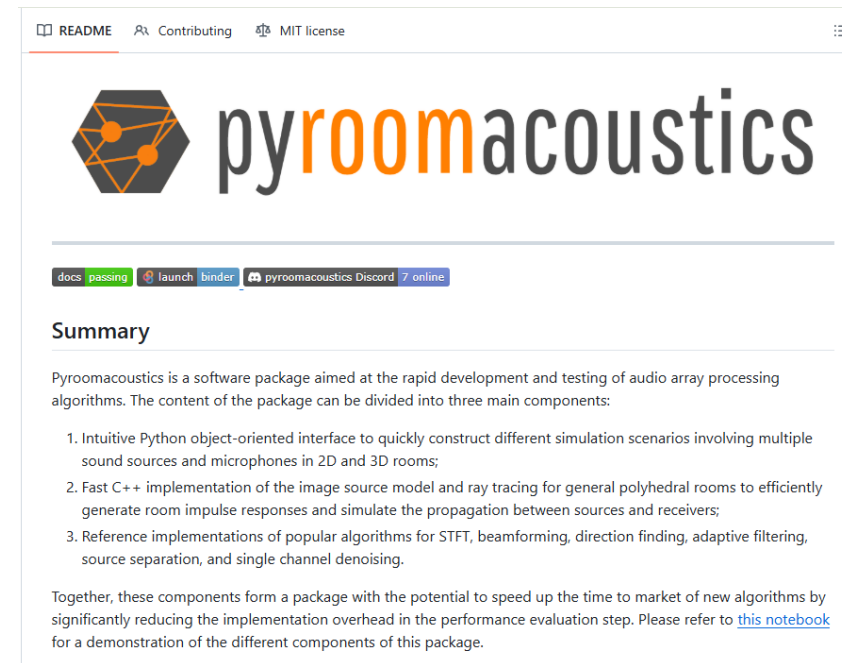


# Sound Propagation System: Impulse Response

- Sound Simulation (Python)
  - Habitat2.0 – SoundSpace2.0 (META)
  - Pyroomacoustics



Habitat2.0



Pyroomacoustics